

B.L.D.E. Association's

VACHANA PITAMAHA DR.P.G.HALAKATTI
COLLEGE OF ENGINEERING AND TECHNOLOGY, VIJAYAPUR
LIBRARY AND INFORMATION CENTER

**QUESTION PAPERS** 

1<sup>st</sup> & 2<sup>nd</sup>.SEMESTER

M.TECH

**ELETRICAL & ELETRONIC** 

DEC.2018/JAN2019

B.L.D.E. ASSOCIATION'S
VACHANA PITAMAHA
DR.P.G.HALAKATTI
COLLEGE OF ENGINEERING
LIBRARY, BIJAPUR.

B.L.D.E DR.P.G.HALAKATTI COLLEGE OF ENGINEERING AND TECHNOLOGY, LIBRARY VIJAYAPUR

# **INDEX**

SL No	SUBJECT CODE	TITLE OF THE PAPER	PAGE No
01	18EEE/ESE/EPE/ EPS/ECD/EMS1 1	Mathematical Methods in Control.	1-3
02	18EMS12	Analysis of Linear Systems.	4-6

# First Semester M.Tech. Degree Examination, Dec.2018/Jan.2019 Analysis of Linear Systems

Time: 3 hrs.

Max. Marks: 100

Note: Answer FIVE full questions, choosing ONE full question from each module.

# Module-1

a. Define: i) State ii) State variables iii) State space iv) State trajectory.
b. Determine the state model for the given electrical circuit shown in Fig.Q1(b). (10 Marks)

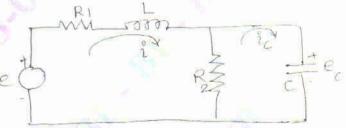


Fig.Q1(b)

c. Show that the state model of a given system is not unique.

(06 Marks)

### OR

2 a. Show that eigen values are invariant under linear transformation.

(04 Marks)

b. Obtain the state model of the system whose transfer function is given by

$$\frac{Y(s)}{U(s)} = \frac{10(s+4)}{s(s+1)(s+3)}.$$

(08 Marks)

c. Construct the state diagrams for the system with TF =  $\frac{Y(s)}{U(s)} = \frac{10}{[s^3 + 4s^2 + 2s + 1]}$ . (08 Marks)

### Module-2

3 a. Explain the digital control system with block diagram.

(08 Marks)

b. Derive pulse transfer function.

(06 Marks)

c. Obtain the pulse transfer function G(z) of the system shown in Fig. 3(c) where  $G(s) = \frac{1}{s+a}$ .



Fig.Q3(c) 1 of 3

(06 Marks)

4 a. What are quantizing and quantization error? Explain in brief.

(08 Marks)

b. Obtain the diagonal canonical form of state model for the system represented by the difference equation: y(k + 2) + 5y(k + 1) + 6y(k) = u(k). Assume zero initial conditions.

(06 Marks)

c. Obtain the state model for the system shown in Fig.Q4(c).

(06 Marks)

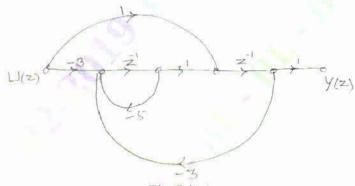


Fig.Q4(c)

# Module-3

- 5 a. Evaluate state transition matrix using:
  - i) Lapalce transform method
  - ii) Caytey Hamilton method

For the system with  $A = \begin{bmatrix} 0 & 2 \\ -2 & -4 \end{bmatrix}$ . (12 Marks)

b. Derive pulse transfer function matrix.

(08 Marks)

### OR

6 a. Obtain for the discrete time state equation state transition matrix:

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -0.16 & -1 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}.$$
 (10 Marks)

b. Compute time response of the system given by:

$$\overset{\circ}{\mathbf{x}}(\mathbf{t}) = \begin{bmatrix} 0 & 1 \\ -2 & 0 \end{bmatrix} \mathbf{x}(\mathbf{t}); \ \mathbf{x}(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \text{ and } \mathbf{y}(\mathbf{t}) = \begin{bmatrix} 1 -1 \end{bmatrix} \mathbf{x}(\mathbf{t}).$$
 (10 Marks)

### Module-4

7 a. Check controllability and observability for the following system:

$$\mathbf{A} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & -2 & -3 \end{bmatrix}; \ \mathbf{B} = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \ C = \begin{bmatrix} 3 & 4 & 1 \end{bmatrix}.$$
 (10 Marks)

 Explain controllability and observability tests of state model in Jord canonical form for discrete time systems.

2 of 3

- 8 a. Explain in brief loss of controllability and observability due to sampling. (08 Marks)
  - b. Consider a system described by the state equation  $\dot{x}(t) = Ax(t) + bu(t)$ , where

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}; B = \begin{bmatrix} -1 \\ 1 \\ 1 \end{bmatrix}$$
 check for controllability of the system. (06 Marks)

c. Show that the following system is not completely observable:

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix} y(k) = \begin{bmatrix} 0 & 1 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}.$$
 (06 Marks)

# Module-5

9 a. The plant model is given by:

$$X = AX + bu$$
 with  $A = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}$   $b = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$ 

Calculate the state feedback gain matrix 'K' where the desired pole locations are at  $S = -4 \pm i4$ . (10 Marks)

b. For a single input system, derive the expressions for transformation matrix 'P' which puts the system matrix 'A' in controllable companion form. (10 Marks)

### OR

10 a. Write a note on full order state observer with block diagram.

- (10 Marks)
- b. For the single input single output system  $\mathring{x} = \begin{bmatrix} 0 & 1 \\ 1 & -2 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$   $y = \begin{bmatrix} 1 & 2 \end{bmatrix} x$ , check wherever system remains controllable and observable after introducing a feedback signal  $u = r + \begin{bmatrix} 2 & -1 \end{bmatrix} x$ .

\* \* \* \* \*

# First Semester M.Tech. Degree Examination, Dec.2018/Jan.2019 Analysis of Linear Systems

Time: 3 hrs.

Max. Marks: 100

Note: Answer FIVE full questions, choosing ONE full question from each module.

# Module-1

- 1 a. Define: i) State ii) State variables iii) State space iv) State trajectory. (04 Marks)
  - b. Determine the state model for the given electrical circuit shown in Fig.Q1(b). (10 Marks)

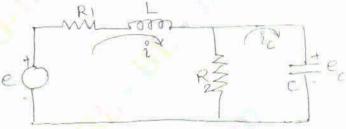


Fig.Q1(b)

c. Show that the state model of a given system is not unique.

(06 Marks)

### OP

- 2 a. Show that eigen values are invariant under linear transformation.
- (04 Marks)
- b. Obtain the state model of the system whose transfer function is given by

$$\frac{Y(s)}{U(s)} = \frac{10(s+4)}{s(s+1)(s+3)}.$$

(08 Marks)

c. Construct the state diagrams for the system with  $TF = \frac{Y(s)}{U(s)} = \frac{10}{[s^3 + 4s^2 + 2s + 1]}$ . (08 Marks)

# Module-2

3 a. Explain the digital control system with block diagram.

(08 Marks)

b. Derive pulse transfer function.

(06 Marks)

c. Obtain the pulse transfer function G(z) of the system shown in Fig. 3(c) where  $G(s) = \frac{1}{s+a}$ .

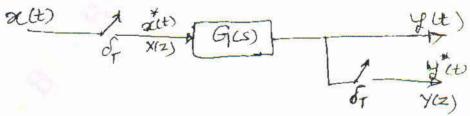


Fig.Q3(c) 1 of 3

(06 Marks)

4 a. What are quantizing and quantization error? Explain in brief.

(08 Marks)

b. Obtain the diagonal canonical form of state model for the system represented by the difference equation: y(k + 2) + 5y(k + 1) + 6y(k) = u(k). Assume zero initial conditions.

(06 Marks)

c. Obtain the state model for the system shown in Fig.Q4(c).

(06 Marks)

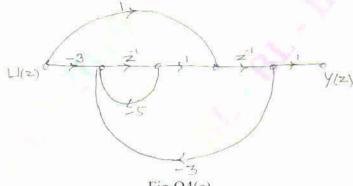


Fig.Q4(c)

# Module-3

- 5 a. Evaluate state transition matrix using:
  - i) Lapalce transform method
  - ii) Caytey Hamilton method

For the system with  $A = \begin{bmatrix} 0 & 2 \\ -2 & -4 \end{bmatrix}$ . (12 Marks)

b. Derive pulse transfer function matrix.

(08 Marks)

### OR

6 a. Obtain for the discrete time state equation state transition matrix:

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -0.16 & -1 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}.$$
 (10 Marks)

b. Compute time response of the system given by:

$$\overset{\circ}{\mathbf{x}}(\mathbf{t}) = \begin{bmatrix} 0 & 1 \\ -2 & 0 \end{bmatrix} \mathbf{x}(\mathbf{t}); \ \mathbf{x}(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \text{ and } \mathbf{y}(\mathbf{t}) = \begin{bmatrix} 1 -1 \end{bmatrix} \mathbf{x}(\mathbf{t}).$$
 (10 Marks)

### Module-4

7 a. Check controllability and observability for the following system:

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & -2 & -3 \end{bmatrix}; B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} C = \begin{bmatrix} 3 & 4 & 1 \end{bmatrix}.$$
 (10 Marks)

 Explain controllability and observability tests of state model in Jord canonical form for discrete time systems.

2 of 3

- Explain in brief loss of controllability and observability due to sampling. (08 Marks)
  - Consider a system described by the state equation  $\dot{x}(t) = Ax(t) + bu(t)$ , where

Consider a system described by the state equation 
$$x(t) = Ax(t) + bu(t)$$
, where
$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}; B = \begin{bmatrix} -1 \\ 1 \\ 1 \end{bmatrix} \text{ check for controllability of the system.}$$
(06 Marks)

Show that the following system is not completely observable:

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix} y(k) = \begin{bmatrix} 0 & 1 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}. \tag{06 Marks}$$

# Module-5

a. The plant model is given by:

$$\overset{\circ}{X} = AX + bu \text{ with } A = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} b = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

Calculate the state feedback gain matrix 'K' where the desired pole locations are at  $S = -4 \pm i4$ .

b. For a single input system, derive the expressions for transformation matrix 'P' which puts (10 Marks) the system matrix 'A' in controllable companion form.

### OR

Write a note on full order state observer with block diagram. 10

(10 Marks)

For the single input single output system  $\hat{x} = \begin{bmatrix} 0 & 1 \\ 1 & -2 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$   $y = \begin{bmatrix} 1 & 2 \end{bmatrix} x$ , check wherever system remains controllable and observable after introducing a feedback signal (10 Marks) u = r + [2 -1]x.